

DTIC FULL COPY

4

233  
AD-A217

**David Taylor Research Center**

Bethesda, MD 20084-5000

**DTRC-SME-89/67 September 1989**

Ship Materials Engineering Department  
Research & Development Report

DTRC-SME-89/67 Through-Thickness Strain Response of Thick Composites in Compression

**Through-Thickness Strain Response of  
Thick Composites in Compression**

by  
E.T. Camponeschi, Jr.



Approved for public release; distribution unlimited.

60 01 00 00

## MAJOR DTRC TECHNICAL COMPONENTS

CODE 011 DIRECTOR OF TECHNOLOGY, PLANS AND ASSESSMENT

- 12 SHIP SYSTEMS INTEGRATION DEPARTMENT
- 14 SHIP ELECTROMAGNETIC SIGNATURES DEPARTMENT
- 15 SHIP HYDROMECHANICS DEPARTMENT
- 16 AVIATION DEPARTMENT
- 17 SHIP STRUCTURES AND PROTECTION DEPARTMENT
- 18 COMPUTATION, MATHEMATICS & LOGISTICS DEPARTMENT
- 19 SHIP ACOUSTICS DEPARTMENT
- 27 PROPULSION AND AUXILIARY SYSTEMS DEPARTMENT
- 28 SHIP MATERIALS ENGINEERING DEPARTMENT

### DTRC ISSUES THREE TYPES OF REPORTS:

1. **DTRC reports, a formal series**, contain information of permanent technical value. They carry a consecutive numerical identification regardless of their classification or the originating department.
2. **Departmental reports, a semiformal series**, contain information of a preliminary, temporary, or proprietary nature or of limited interest or significance. They carry a departmental alphanumerical identification.
3. **Technical memoranda, an informal series**, contain technical documentation of limited use and interest. They are primarily working papers intended for internal use. They carry an identifying number which indicates their type and the numerical code of the originating department. Any distribution outside DTRC must be approved by the head of the originating department on a case-by-case basis.

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE

REPORT DOCUMENTATION PAGE

1a. REPORT SECURITY CLASSIFICATION Unclassified		1b. RESTRICTIVE MARKINGS	
2a. SECURITY CLASSIFICATION AUTHORITY		3. DISTRIBUTION/AVAILABILITY OF REPORT Approved for public release; distribution unlimited.	
2b. DECLASSIFICATION/DOWNGRADING SCHEDULE			
4 PERFORMING ORGANIZATION REPORT NUMBER(S) DTRC-SME-89/67		5. MONITORING ORGANIZATION REPORT NUMBER(S)	
6a. NAME OF PERFORMING ORGANIZATION David Taylor Research Center	6b. OFFICE SYMBOL (If applicable) Code 2802	7a. NAME OF MONITORING ORGANIZATION	
6c. ADDRESS (City, State, and ZIP Code) Annapolis, MD 21402-5067		7b. ADDRESS (City, State, and ZIP Code)	
8a. NAME OF FUNDING/SPONSORING ORGANIZATION David Taylor Research Center	8b. OFFICE SYMBOL (If applicable) Code 0113	9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER	
8c. ADDRESS (City, State, and ZIP Code) Bethesda, MD 20084-5000		10. SOURCE OF FUNDING NUMBERS PROGRAM ELEMENT NO. 61152N	PROJECT NO. TASK NO. WORK UNIT ACCESSION NO. 1720-476
11. TITLE (Include Security Classification) (U) Through-Thickness Strain Response of Thick Composites in Compression			
12. PERSONAL AUTHOR(S) Eugene T. Camponeschi, Jr.			
13a. TYPE OF REPORT RDT&E	13b. TIME COVERED FROM 8/87 TO 8/89	14. DATE OF REPORT (Year, Month, Day) 1989 Sept 5	15. PAGE COUNT 39
16. SUPPLEMENTARY NOTATION			

17. COSATI CODES FIELD      GROUP      SUB-GROUP	18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number) Composite Materials, Thick-Section, Compression, 3-D Properties
---	---

19. ABSTRACT (Continue on reverse if necessary and identify by block number)

With the continued success of composite materials in high performance structures, new applications for Navy primary structure are being identified. Many of these applications require designs with composite materials having section thicknesses greater than those that have been used and studied to date. Along with this interest in thick composite structures comes the need for full three-dimensional stress analysis. The limits and accuracy of existing three-dimensional data bases will dictate the limit and accuracy of corresponding analyses.

This report summarizes an investigation of the through-thickness strain response of thick composite materials subjected to compressive loading. One-half inch thick (96 ply) carbon and S2 glass reinforced composites were studied. A thick-section compression test method has been developed for the purposes of this investigation. Using this test method the longitudinal and through-thickness

20. DISTRIBUTION/AVAILABILITY OF ABSTRACT <input type="checkbox"/> UNCLASSIFIED/UNLIMITED <input checked="" type="checkbox"/> SAME AS RPT. <input type="checkbox"/> DTIC USERS	21. ABSTRACT SECURITY CLASSIFICATION Unclassified	
22a. NAME OF RESPONSIBLE INDIVIDUAL E.T. Camponeschi, Jr.	22b. TELEPHONE (Include Area Code) (301) 267-2165	22c. OFFICE SYMBOL Code 2802

*CON-X*  
Unclassified

SECURITY CLASSIFICATION OF THIS PAGE

strain to failure, longitudinal modulus, inplane and through-thickness Poisson's ratio, and ultimate strength of these materials have been determined. The through-thickness data from the 96 ply [0] coupons show the materials to be transversely isotropic. The through-thickness data from 96 ply [0/0/90] laminates show good correlation with a theoretical solution that provides the nine elastic constants for thick orthotropic plates. (A-6)



Accession For	
NTIS CRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By _____	
Distribution / _____	
Availability Codes	
Dist	1. AVAL. AND / OR Special
A-1	

Unclassified  
SECURITY CLASSIFICATION OF THIS PAGE

## CONTENTS

ABBREVIATIONS.....	v
ABSTRACT.....	1
ADMINISTRATIVE INFORMATION.....	1
INTRODUCTION.....	1
EXPERIMENTAL PROCEDURE.....	3
DESCRIPTION OF TEST METHOD.....	3
MATERIAL SYSTEMS.....	5
SPECIMEN GEOMETRY.....	7
THROUGH-THICKNESS POISSON'S RATIO DETERMINATION.....	10
RESULTS AND DISCUSSION.....	13
CONCLUSIONS.....	28
REFERENCES.....	30
ACKNOWLEDGMENTS.....	30

## FIGURES

1. Schematic of DTRC thick-section compression fixture.....	4
2. Photograph of DTRC thick-section compression fixture....	6
3. Specimen geometry, material directions and strain gage locations.....	9
4. Permissible length/thickness ratios.....	11
5. Longitudinal stress-strain plot - $[0]_{96}$ carbon/epoxy.....	14
6. Longitudinal stress-strain plot - $[0]_{96}$ S2 glass/epoxy.....	15
7. Longitudinal stress-strain plot - $[0/0/90]_{16s}$	

carbon/epoxy.....	16
8. Longitudinal stress-strain plot - [0/0/90] <sub>16s</sub>	
S2 glass/epoxy.....	17
9. Through-thickness versus longitudinal	
strain plot - [0] <sub>96</sub> and [0/0/90] <sub>16s</sub>	
carbon/epoxy.....	18
10. Through-thickness versus longitudinal	
strain plot - [0] <sub>96</sub> and [0/0/90] <sub>16s</sub>	
S2 glass/epoxy.....	19
11. $\text{NU}_{xz}$ sensitivity - carbon/epoxy.....	26
12. $\text{NU}_{xz}$ sensitivity - S2 glass/epoxy.....	27

#### TABLES

1. Specimen designations.....	12
2. AS4/3501-6 longitudinal modulus and Poisson's	
ratio data.....	20
3. S2 Glass/3501-6 longitudinal modulus and Poisson's	
ratio data.....	21
4. Laminate input data for three-dimensional	
elastic constant calculations.....	24
5. Comparison of theoretical and experimental	
$\text{NU}_{xz}$ results.....	25

#### ABBREVIATIONS

C.V.	Coefficient of variation
DTRC	David Taylor Research Center
$E_i$	i-direction modulus of elasticity
FVF	fiber volume fraction
$G_{ij}$	ij-plane shear modulus of elasticity
Msi	one-million pounds per square inch
$\nu_{ij}$	ij-plane Poisson's ratio
psi	pounds per square inch

## ABSTRACT

With the continued success of composite materials in high performance structures, new applications for Navy primary structure are being identified. Many of these applications require designs with composite materials having section thicknesses greater than those that have been used and studied to date. Along with this interest in thick composite structures comes the need for full three-dimensional stress analysis. The limits and accuracy of existing three-dimensional data bases will dictate the limit and accuracy of corresponding analyses.

This report summarizes an investigation of the through-thickness strain response of thick composite materials subjected to compressive loading. One-half inch thick (96 ply) carbon and S2 glass reinforced composites were studied. A thick-section compression test method has been developed for the purposes of this investigation. Using this test method the longitudinal and through-thickness strain to failure, longitudinal modulus, inplane and through-thickness Poisson's ratio, and ultimate strength of these materials have been determined. The through-thickness data from the 96 ply [0] coupons show the materials to be transversely isotropic. The through-thickness data from 96 ply [0/0/90] laminates show good correlation with a theoretical solution that provides the nine elastic constants for thick orthotropic plates.

## ADMINISTRATIVE INFORMATION

This work was performed as a DTRC Independent Research Program, sponsored by the Office of Naval Research and administered by the Research Director, DTRC 0113, under Program Element 61152N and Work Unit 1-1720-476.

## INTRODUCTION

The compressive response of fiber-reinforced composite materials has been the subject of numerous investigations over the past 25 years. Although these investigations have improved the understanding of how these materials respond to compressive loads, the emphasis of these investigations have been on materials less than 0.25 inches thick [1].

With the continued success of composites in high performance structures and the reduction of fabricated costs due to improved manufacturing methods, more applications are being identified. Many of these applications require design of composite materials with section thicknesses greater than those with which engineers have design experience and confidence. Increases in required material thicknesses requires additional analysis procedures at both the material level and the structural level.

In many instances two-dimensional stress analyses will not be appropriate in analyzing thick composite materials and structures. Three-dimensional analysis requires full three-dimensional material characterization. The limits and accuracy of existing three-dimensional data bases will dictate the limit and accuracy of corresponding analyses.

In light of the need for three-dimensional materials characterization, this paper summarizes an investigation of the through-thickness strain response of thick composite materials subjected to compressive loading.

## EXPERIMENTAL PROCEDURE

### DESCRIPTION OF TEST METHOD

In order to evaluate the through-thickness strain response of composite coupons, a specimen thickness of 0.5 inches thick was necessary. The development of a fixture to test these specimens in compression was necessary and the following criteria were applied: the fixture must allow thick-section testing capability beginning at 0.25 inches, must allow further scale up for thicker, wider, and longer specimens, must prevent load eccentricities, must allow an unsupported gage length, and must prevent splitting or brooming failures from occurring near the load introduction points.

A cross section of the fixture designed to meet the above criteria is shown in Fig. 1. Load is introduced through the end of the specimen. This method of load introduction is more desirable for thick composites than shear load introduction since transfer of load through shear would require large tabbed areas to reduce the shear stress in the tab adhesive. The size, complexity and resulting expense of fixtures designed to introduce load through shear precluded their design and use for this program.

The clamping blocks on the ends of the specimen are held secure to the specimen by through-bolts that provide appropriate clamping force. A hardened steel plate is inserted between both ends of the specimen and the test machine crosshead platens and

## DTRC THICK-SECTION COMPRESSION TEST METHOD

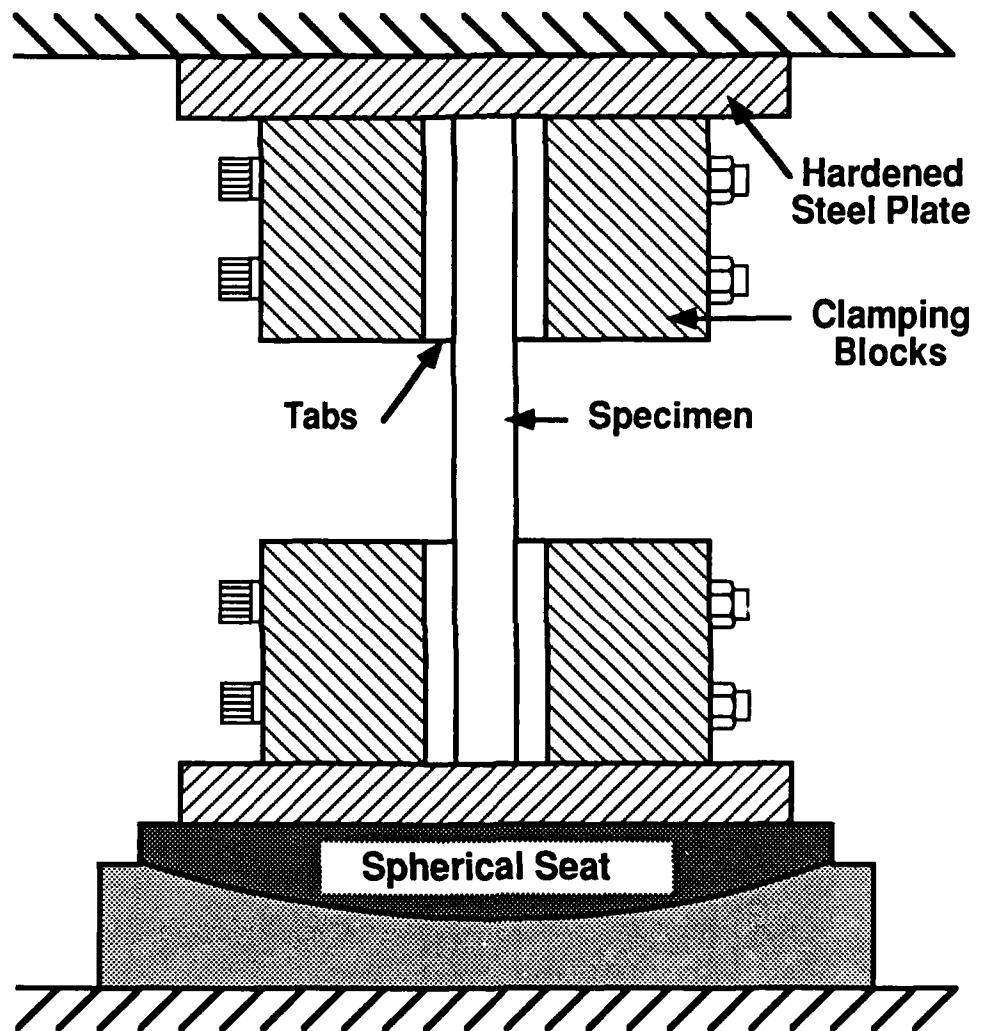


Fig. 1. Schematic of DTRC thick-section compression fixture.

act as load bearing surfaces. A self aligning spherical seat is placed between one end of the specimen and the load machine to assist in aligning the specimen axis and the loading axis.

To load the specimen into the fixture for testing, two mating clamping blocks that comprise one-half of the fixture are placed on one of the hardened steel loading plates. The specimen is placed into this half of the fixture and when the end contacts the plate the clamping bolts are tightened. The other end of the specimen is clamped into the other half of the fixture using the same procedure. The specimen and both halves of the fixture now become one unit and this unit is placed in the test machine for the application of load. A specimen with the clamping blocks attached to one end is shown in Fig. 2.

The geometry of the specimens for this investigation were adequate to support the weight of the clamping blocks without alignment rods.

#### MATERIAL SYSTEMS

Two material systems were evaluated in this investigation. They were chosen to investigate the effects of carbon and glass fiber reinforcements in a common epoxy matrix (Hercules 3501-6). The effect of fiber sizing and the resulting interface chemistry will also affect the compressive response of thick composites however these effects were not quantified in this investigation.

The carbon reinforced prepreg tape was supplied by Hercules

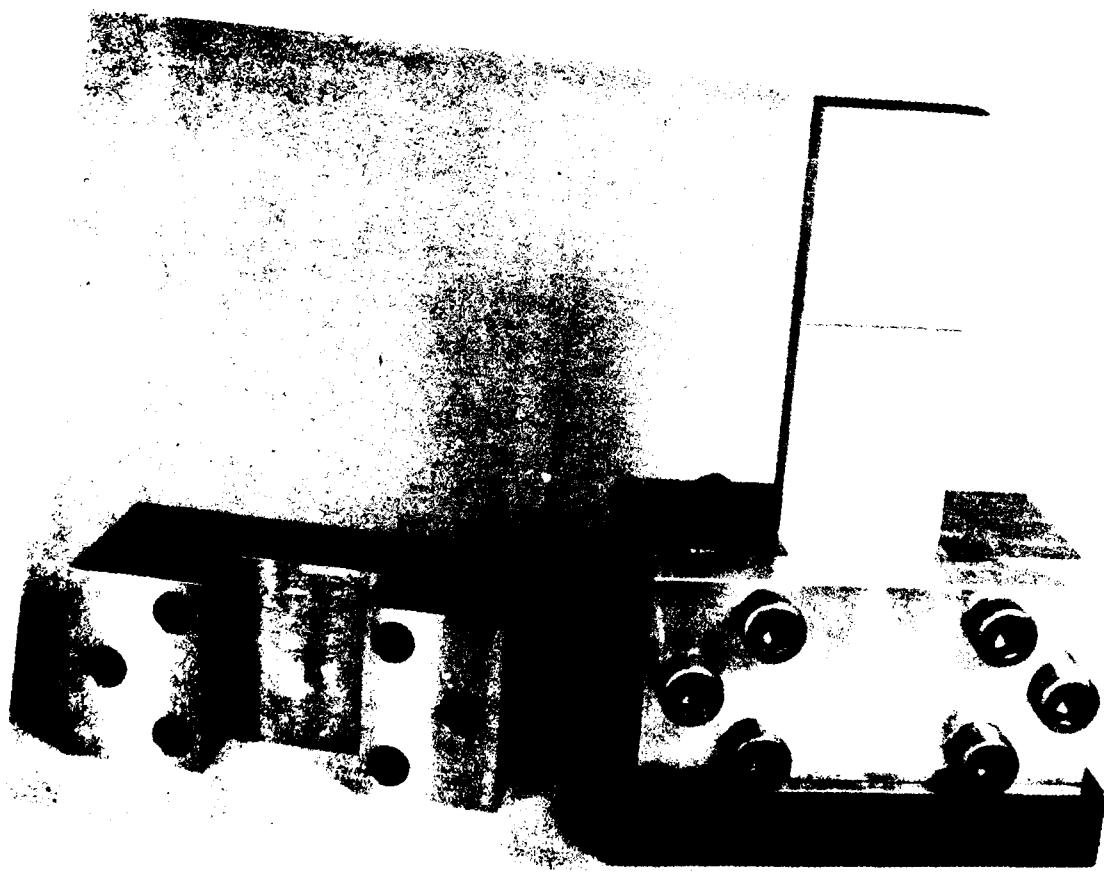


Fig. 2. Photograph of DTRC thick-section compression fixture.

Inc. and was AS4 fiber with 3501-6 350° F epoxy resin. The S2 glass reinforced prepreg was supplied by Fiberite and was S2 glass fiber also with 3501-6 350 F epoxy resin. Both systems were supplied as 12 inch wide prepreg tape and were autoclave cured at DTRC. An autoclave air temperature schedule that was slightly different than those used for thin (< 0.25 inch) epoxy based composites was used. This air temperature was determined from test cures on 96 ply laminates with thermocouples placed in three locations within the test panels.

Following fabrication, samples from each of the four panels (two AS4/3501-6 and two S2 glass/3501-6) were removed and tested for fiber volume fraction (FVF) and void content (ASTM D3171 and D2734). The fiber volume fraction of the AS4/3501-6 panels averaged 60.0 % and the void content averaged 0.34 %. The fiber volume fraction of the S2 glass/3501-6 panels averaged 53.8 % and the void content averaged 0.97 %.

#### SPECIMEN GEOMETRY

Specimens for this investigation were machined from 12 inch by 12 inch panels, 96 plies thick, of two laminate stacking sequences. The cured laminates were machined so unidirectional  $[0]_{96}$  and crossply  $[0_2/90]_{16s}$  specimens were available for both the carbon and S2 glass reinforced laminates. The nominal specimen dimensions were 2.00 inches wide by 0.5 inches thick by either 6.5 or 7.5 inches long. The tab length was 2.5 inches so the 6.5 inch long specimen had a 0.75 inch gage length and the

7.5 inch specimen had a 2.5 inch gage length. The specimen geometry is shown in Fig. 3. The average specimen thickness was 0.530 inches for the AS4 specimens and 0.570 inches for the S2 glass specimens. The average tab thickness was 0.090 for the AS4 specimens and 0.070 for the S2 glass specimens.

The length of the specimen gage section was selected on the basis of a Euler column buckling analysis. The materials elastic constants and specimen geometry is used to determine the maximum stable gage length. The equation to determine this permissible length-to-thickness ratio can be expressed as follows:

$$\frac{l}{t} = 0.9069 \left[ \frac{E_x}{Y_{ult}} \right]^{\frac{1}{2}}$$

where

$l$  = specimen length

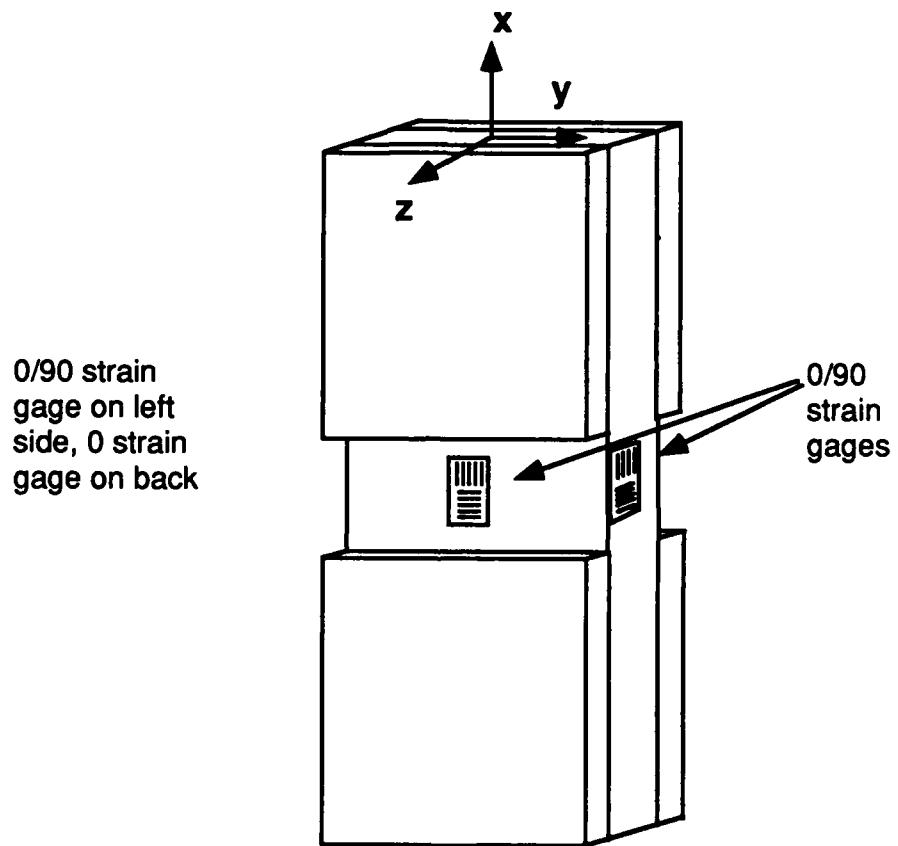
$E_x$  = longitudinal modulus

$t$  = specimen thickness

$Y_{ult}$  = ultimate compressive strength

This equation is derived from reference 2 and includes the assumptions that the specimen acts as a pinned end column, the most conservative end fixity assumption. For a material that has a high longitudinal modulus to longitudinal shear modulus ratio the effects of transverse shear can significantly effect column stability. When the effects of transverse shear are included in the above analysis a more conservative maximum gage length is determined and the expression for length/thickness including this

## SPECIMEN GEOMETRY



Specimen Thickness:  $t$   
Width:  $4t$   
Gage Length:  $5t, 3t$

Tab length:  $5t, 2.5$  in. min.  
Thickness:  $.25t, .125$  in. min.

Fig. 3. Specimen geometry, material directions, and strain gage locations.

effect is:

$$\frac{l}{t} = 0.9069 \left[ \frac{E_x}{Y_{ult}} \left( 1 - 1.2 \frac{Y_{ult}}{G_{xz}} \right) \right]^{\frac{1}{2}}$$

where

$l$  = specimen length

$E_x$  = longitudinal modulus

$t$  = specimen thickness

$G_{xz}$  = through-thickness shear modulus

$Y_{ult}$  = ultimate compressive strength

A plot showing the permissible  $l/t$  ratios for an assumed longitudinal modulus and strength is shown in Fig. 4.

Sixteen specimens were fabricated and evaluated for this investigation. Eight specimens were instrumented with seven strain gages and used to monitor strain response on both faces and both free edges of the specimens. The remaining eight were instrumented with two gages (front and back) and used to monitor longitudinal strain on both faces of the specimens. The designations and descriptions for all 16 specimens are shown in Table 1.

#### THROUGH-THICKNESS POISSON'S RATIO DETERMINATION

The thickness of the 96 ply coupons investigated allowed the direct determination of  $\nu_{xz}$  with electrical resistance strain gages.  $\nu_{xz}$  is defined as the through-thickness Poisson's ratio or the negative ratio of the  $z$  direction strain to the  $x$  direction strain when a uniaxial load is applied in the  $x$  direction. Figure 3 shows the  $x$ ,  $y$ , and  $z$  specimen directions

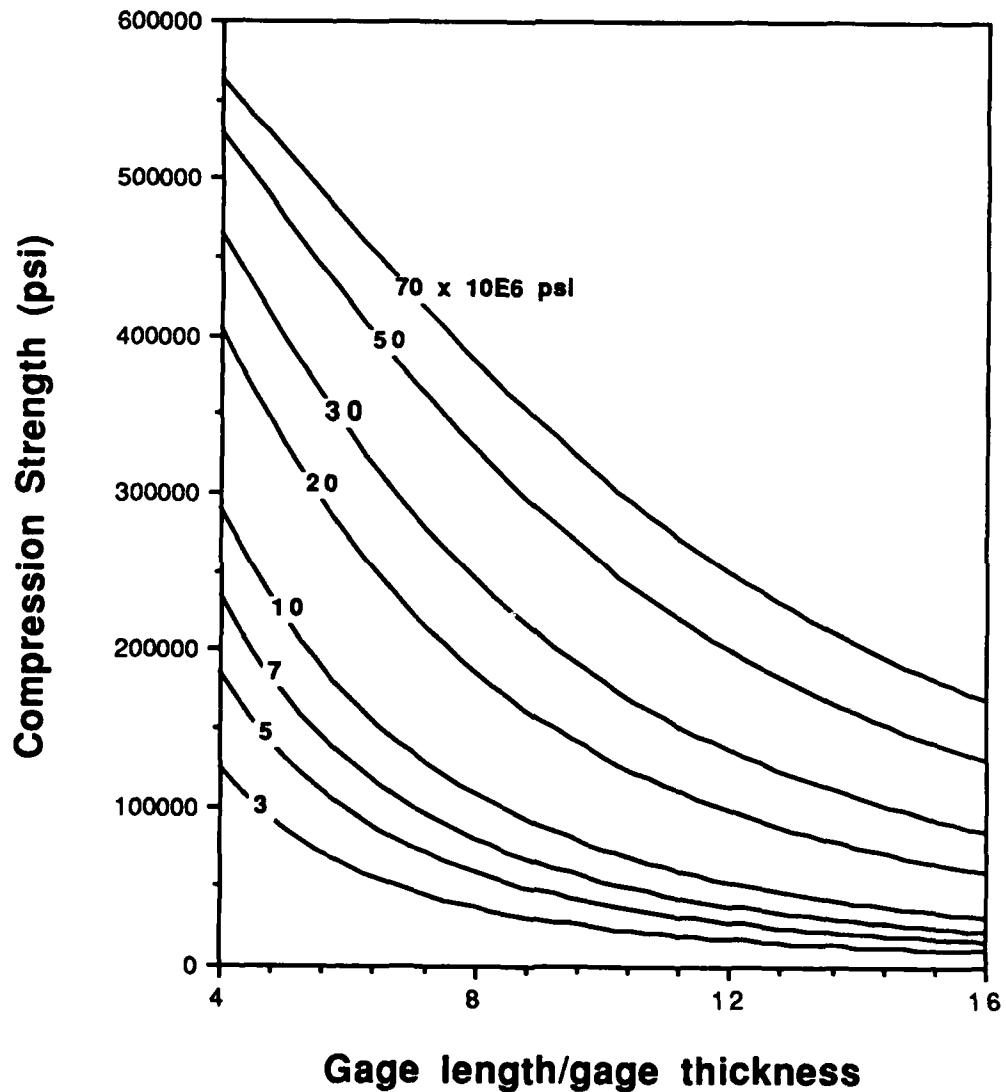


Fig. 4. Permissible length/thickness ratios.

and the strain gage locations. For the  $[0]_{96}$  specimens the specimen Poisson's ratio (NUxz) measured is the same as a lamina Poisson's ratio (NU13). For the 8 specimens in which through-thickness strain was monitored strain gages were mounted on the front and back faces and both edges of each specimen. CEA-06-125UT-350 0/90 gages were placed on both edges and one surface of each specimen and a CEA-06-250UW-350 unidirectional gage was placed on the other surface of the specimen. Strain was

Table 1. Specimen Designation

Specimen	Reinforcement	Orientation	l/t Ratio	Comments
C0A	Carbon	$[0]_{96}$	5:1	7 gages
C0B	Carbon	"	5:1	2 gages
C0C	Carbon	"	3:1	7 gages
C0D	Carbon	"	3:1	2 gages
C9A	Carbon	$[0_2/90]_{16s}$	5:1	7 gages
C9B	Carbon	"	5:1	2 gages
C9C	Carbon	"	3:1	2 gages
C9D	Carbon	"	3:1	7 gages
G0A	S2-Glass	$[0]_{96}$	5:1	7 gages
G0B	S2-Glass	"	5:1	2 gages
G0C	S2-Glass	"	3:1	7 gages
G0D	S2-Glass	"	3:1	2 gages
G9A	S2-Glass	$[0_2/90]_{16s}$	5:1	7 gages
G9B	S2-Glass	"	5:1	2 gages
G9C	S2-Glass	"	3:1	2 gages
G9D	S2-Glass	"	3:1	7 gages

monitored with Micromeasurements 2310 conditioner amplifiers and recorded along with load using a digital data acquisition program running on an IBM-AT computer.

Prior to conducting test to failure, a series of five repetitive tests were run to approximately 25% of the ultimate strain to failure. These tests were run to evaluate the fixture and determine repeatability of data from one test to the next. Between each repetition the specimen and fixture were removed from the test machine, the fixture bolts loosened, the specimen was reinserted into the fixture, and the specimen and fixture were placed into the test machine for the next test. For the first three test repetitions edge strains and load were recorded. Load and surface strains were recorded for the final two repetitions. Each specimen was then loaded monotonically to failure while all seven channels of strain and load were recorded.

#### RESULTS AND DISCUSSION

The results of the repetitive tests run on each of the eight specimens with seven channels of strain indicate that the variation in data from strain gage to strain gage and from test run to test run are within the accuracy of the data from specimen to specimen. The specimen to specimen accuracy is shown in Table 2. with 7.2 % as the largest coefficient of variation for the AS4/3501-6 [0/0/90]<sub>16s</sub> specimens.

Representative stress-strain to failure plots for each of the four laminate/material combinations are shown in Figs. 5-8. Longitudinal stress-strain plots from the specimens instrumented with three (0/90) gages and one (0) gage contain four curves, one

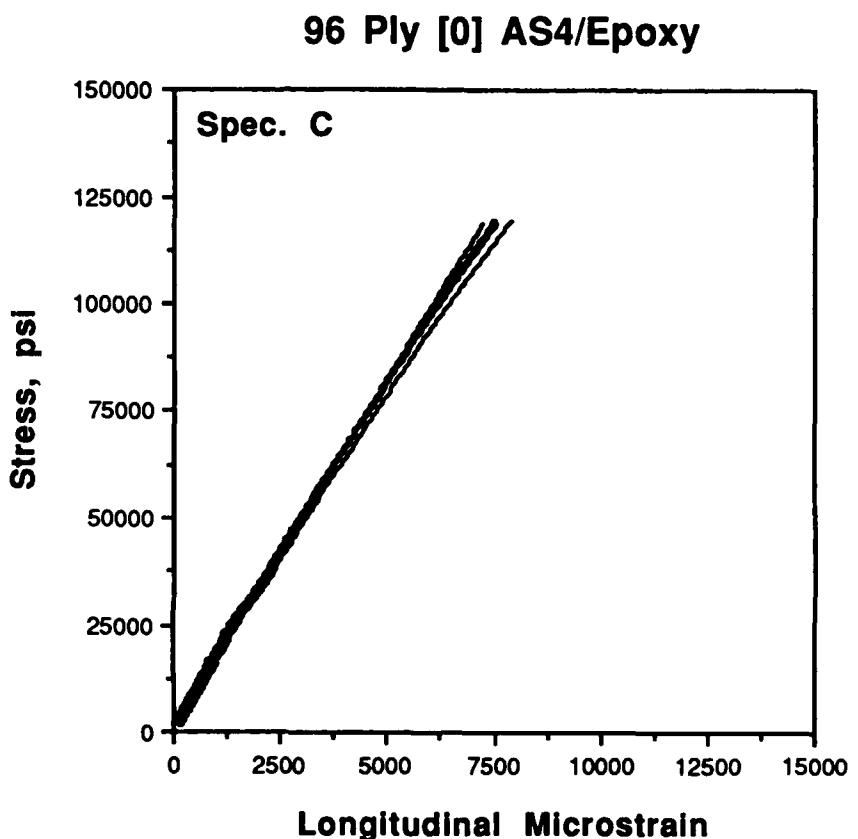
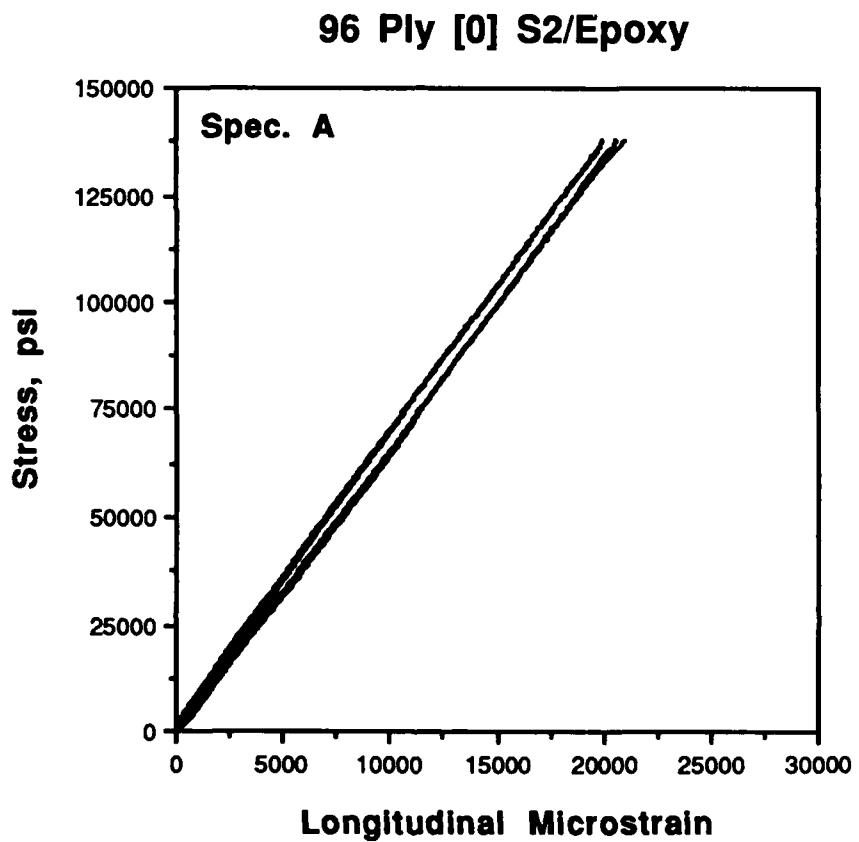
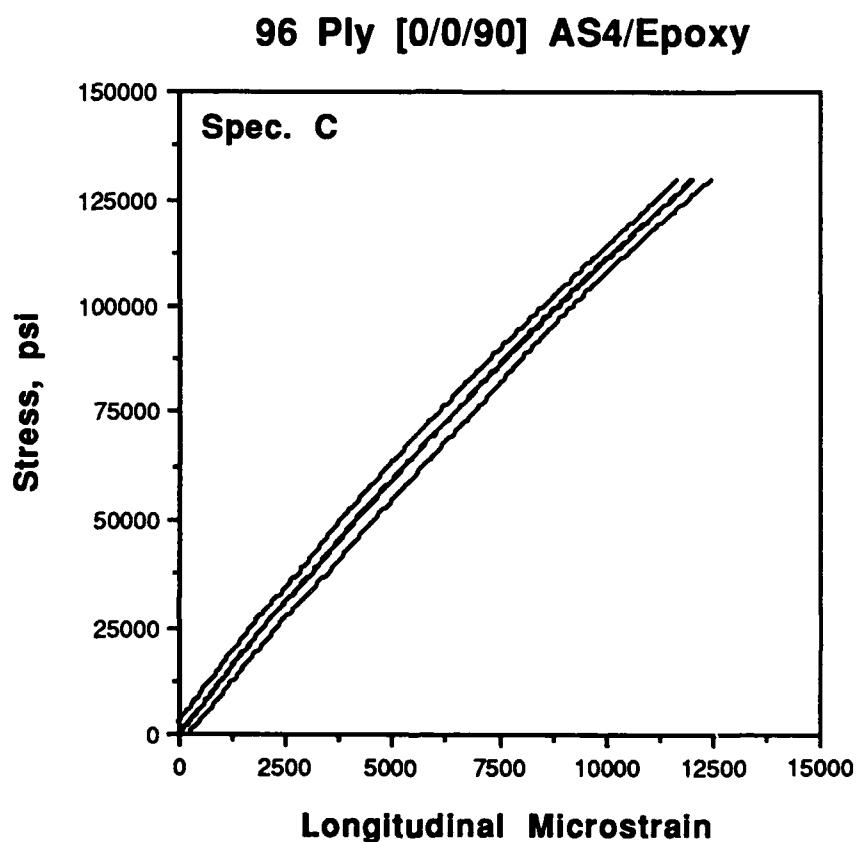


Fig. 5. Longitudinal stress-strain plot -  $[0]_{96}$  carbon/epoxy.



**Fig. 6. Longitudinal stress-strain plot - [0]<sub>96</sub> S2 glass/epoxy.**



**Fig. 7. Longitudinal stress-strain plot -  $[0/0/90]_{16s}$  carbon/epoxy.**

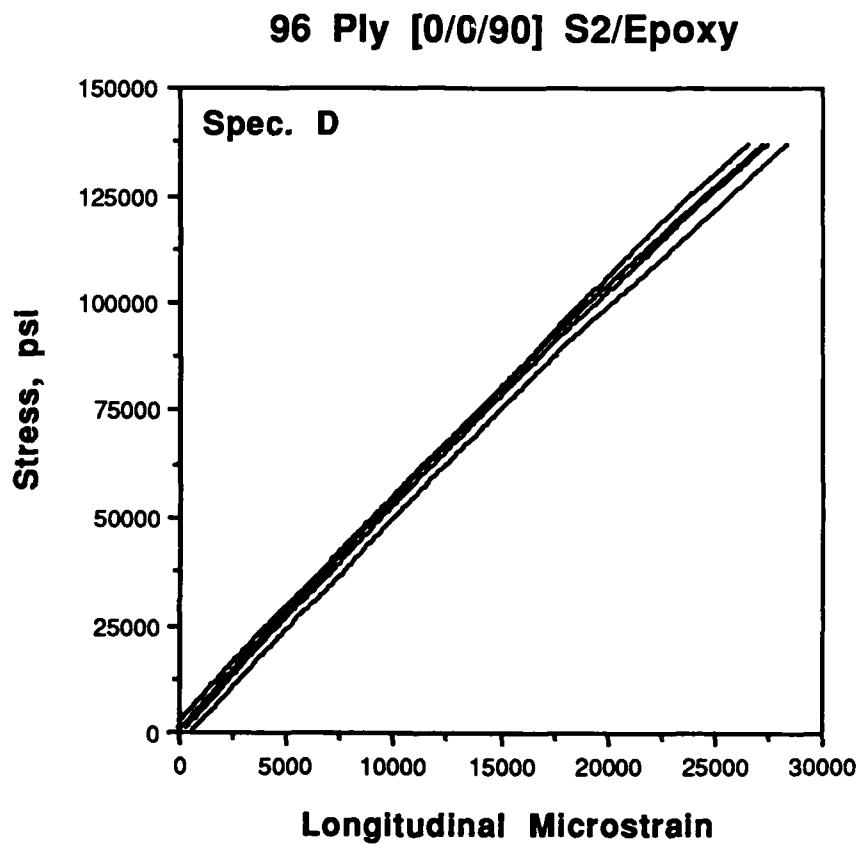


Fig. 8. Longitudinal stress-strain plot -  $[0/0/90]_{16s}$   
S2 glass/epoxy.

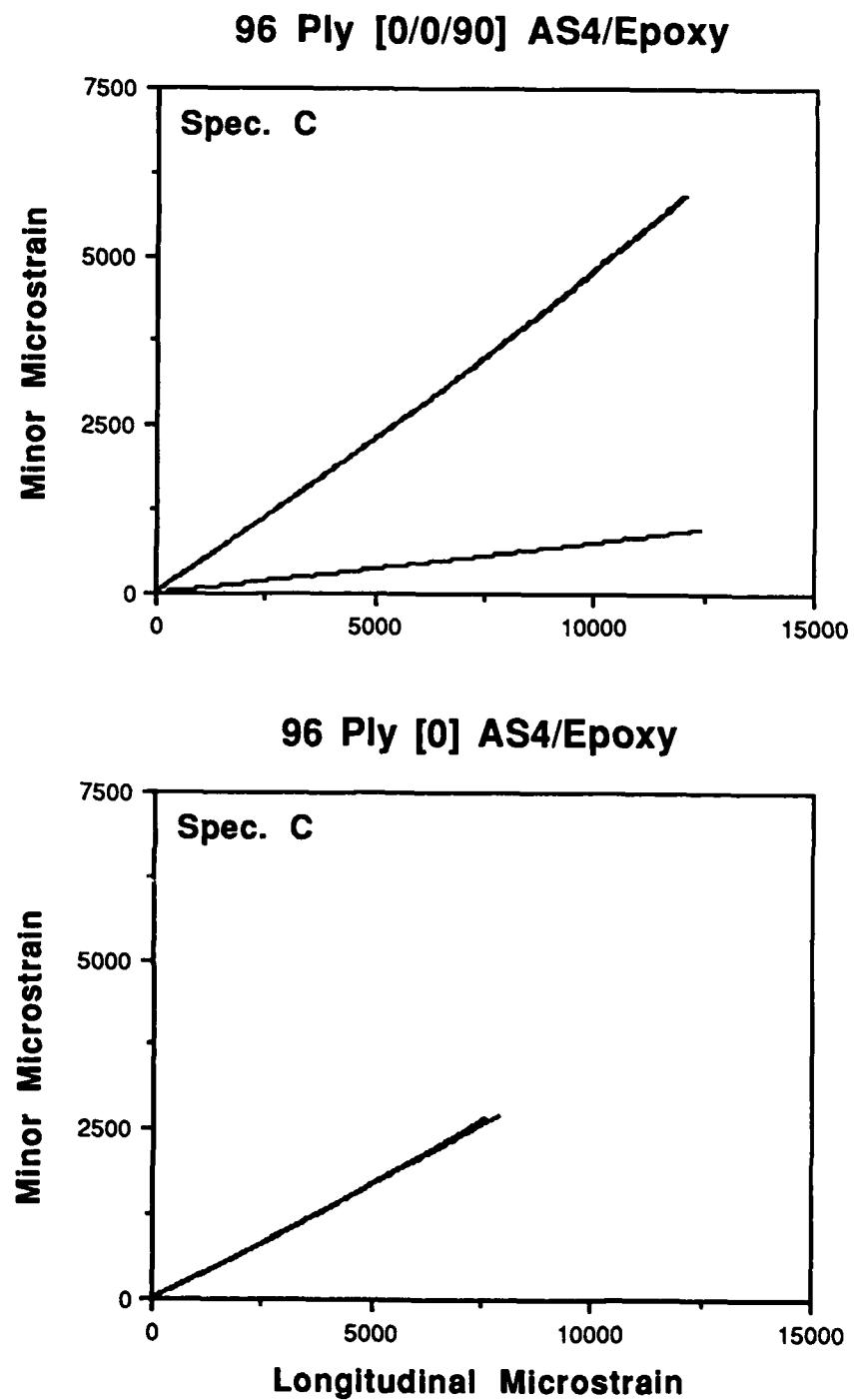


Fig. 9. Through-thickness versus longitudinal strain plot -  $[0]_{96}$  and  $[0/0/90]_{16s}$  carbon/epoxy.

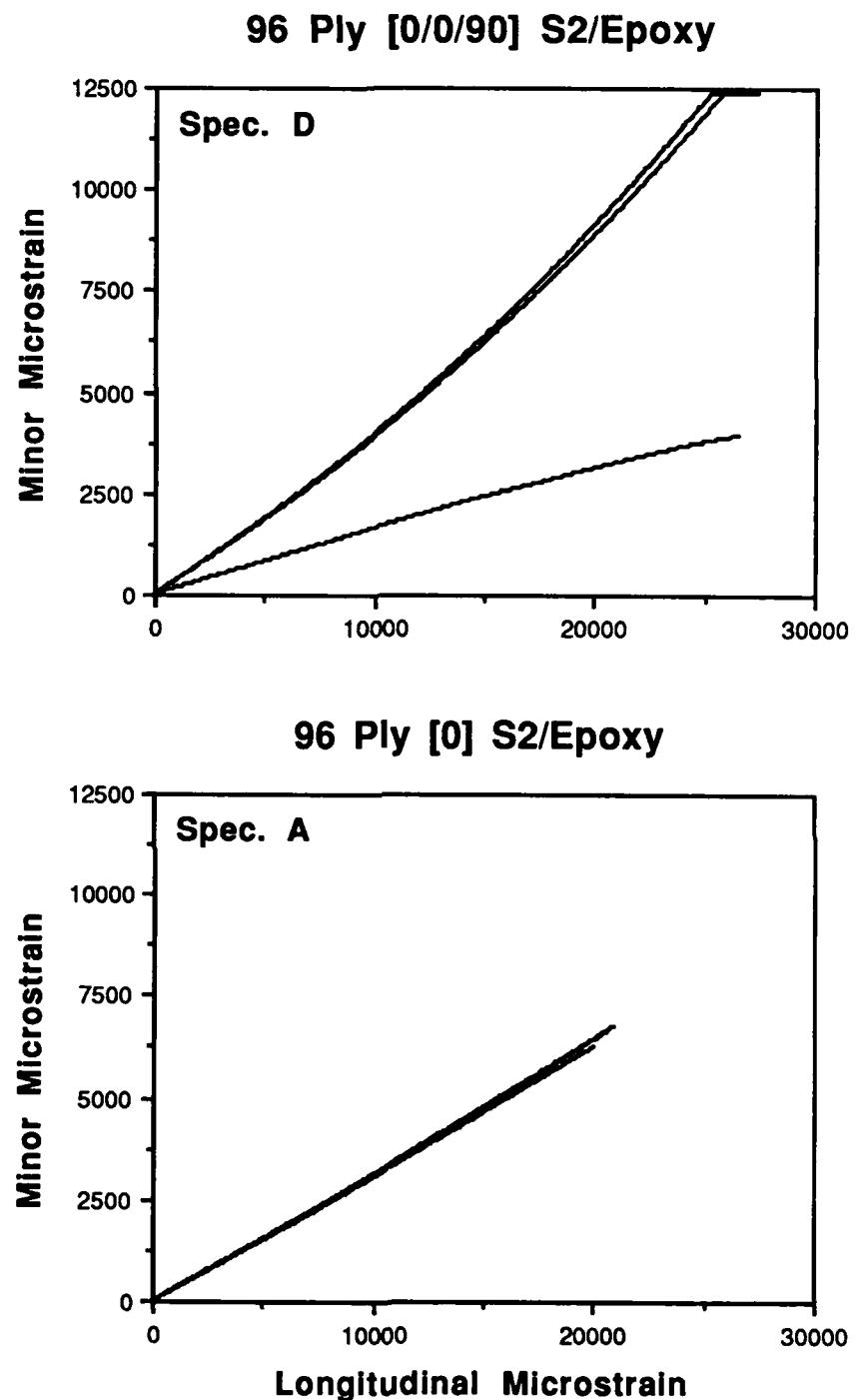


Fig. 10. Through-thickness versus longitudinal strain plot -  $[0]_{96}$  and  $[0/0/90]_{16s}$  S2 glass/epoxy.

for each longitudinal (0 degree) gage. The longitudinal modulus was determined from the slope of these curves. The Poisson's ratio curves (Figs. 9 and 10) contain three curves each, a longitudinal strain versus transverse strain for the face (0/90) gage, and a longitudinal strain versus through-thickness strain for each of the two edge (0/90) gages. The Poisson's ratio's were determined from the slope of these curves which was determined by taking a secant tangent between 1000 and 3000 longitudinal microstrain.

Tables 2 and 3 summarize the longitudinal moduli and Poisson's ratios for the laminates and materials evaluated. The average longitudinal moduli for each specimen represents the average of either two (2 gages) or fourteen (7 gages) recorded values. The average  $NU_{xz}$  for each specimen represents the average of eight recorded values, and the value of  $NU_{xy}$  represents the average of three recorded values.

A significant observation from the data in Tables 2 and 3 is that the value of  $NU_{13}$  ( $NU_{xz}$ ) for unidirectional carbon and S2 Glass reinforced laminates is equivalent to  $NU_{12}$  ( $NU_{xy}$ ). When three dimensional material constants are not available the assumption that  $NU_{13}$  equals  $NU_{12}$  is typically made, and this data shows that the assumption of transverse isotropy is reasonable. This conclusion has been supported in work done by Knight [3].

Unlike  $NU_{xz}$  for unidirectional specimens,  $NU_{xz}$  for laminates

Table 2. AS4/3501-6 longitudinal modulus and Poisson's ration summary.

	Ave. Long. Mod. (Msi)	C.V. (%)	Ave. NU <sub>XZ</sub>	C.V. (%)	Ave. NU <sub>XY</sub>	C.V. (%)
[0] <sub>96</sub> AS4/3501-6						
C0A	16.70	3.1	.319	2.1	.326	1.9
C0B	16.18	0.9				
C0C	16.84	5.3	.326	1.1	.339	1.6
C0D	15.99	1.5				
Total Ave.	16.68	4.3	.322	2.0	.332	2.8

	[0/0/90] <sub>16s</sub> AS4/3501-6					
C9A	12.10	2.1	.448	0.5	.071	4.5
C9B	11.88	3.7				
C9C	11.80	4.8				
C9D	11.03	3.3	.452	3.4	.063	2.7
Total Ave.	11.60	5.2	.450	2.4	.067	7.2

C.V. = Coefficient of variation.

Table 3. S2 Glass/3501-6 longitudinal modulus and Poisson's ratio summary.

	Ave. Long. Mod. (Msi)	C.V. (%)	Ave. NU <sub>XZ</sub>	C.V. (%)	Ave. NU <sub>XY</sub>	C.V. (%)
[0] <sub>96</sub> S2 Glass/3501-6						
G0A	6.97	4.0	.300	1.4	.304	0.0
G0B	7.06	2.3				
G0C	7.26	5.2	.312	2.4	.277	3.4
G0D	7.09	1.0				
Total Ave.	7.11	4.7	.306	2.8	.290	5.5

	[0/0/90] <sub>16s</sub> S2 Glass/3501-6					
G9A	5.61	2.0	.359	3.5	.162	1.1
G9B	5.41	2.1				
G9C	5.62	3.1				
G9D	5.50	3.5	.367	2.8	.152	5.7
Total Ave.	5.55	2.9	.363	3.3	.157	5.0

C.V. = Coefficient of variation.

cannot be directly compared to any inplane lamina or laminate properties. To evaluate the validity of the recorded values a comparison with theoretical predictions of three dimensional elastic constants can be made. Trethewey et. al. [4] recently reviewed several theories for determining the effective three-dimensional properties of layered anisotropic media. All of the reviewed techniques replace a heterogeneous layered media with an equivalent homogeneous anisotropic media and effectively

represent a set of smeared elastic properties. In this report the theory presented by Pagano [5] is reported in detail and encoded, and the elastic properties determined by this theory are the ones that will be used for comparison here.

The input required for the calculation of three-dimensional laminate properties are a complete set of three dimensional lamina properties. The properties used to compare the experimentally and theoretically determined  $Nu_{xz}$  are listed in Table 4. Table 5 shows a comparison of the theoretical and experimental elastic constants for the  $[0/0/90]_{16s}$  carbon and S2 Glass epoxy laminates studied. The calculated value of  $Nu_{xz}$  was forced to correspond the experimental value through selection of input data. In particular, the two values in Table 4 that were varied were  $NU_{23}$  and  $G_{23}$ . In order to determine the sensitivity of the analysis to the choice of these values a parametric study was performed and the results are shown in Figs. 11 and 12. Both figures show that the value of  $NU_{xz}$  is insensitive to  $G_{23}$  but very dependent on  $NU_{23}$ . The value of  $NU_{23}$  necessary to force the match of the theoretical and experimental  $NU_{xz}$  data are the ones listed in Table 4. These values of  $NU_{23}$  are reasonable since they correspond to values measured experimentally in references [3] and [6]. To determine the value of  $NU_{23}$  consistently with the results of this paper  $[90]_{96}$  specimens could be fabricated, instrumented and tested in the same manner as the thick compression tests discussed in this report.

Table 4. Lamina input data for three-dimensional elastic constant calculations.

	AS4/3501-6 (60% FVF)	S2/3501-6 (54% FVF)
$E_1^*$	16.7 Msi	7.11 Msi
$E_2$	1.5 Msi	1.4 Msi
$E_3$	1.5 Msi	1.4 Msi
$Nu_{12}^*$	.33	.30
$Nu_{13}^*$	.33	.30
$Nu_{23}$	.47	.38
$G_{12}^{**}$	.87 Msi	.98 Msi
$G_{13}$	.87 Msi	.98 Msi
$G_{23}$	.55 Msi	.55 Msi

\* from DTRC thick (0.5 inch thick) compression testing

\*\* from DTRC thin (0.040 inch thick) +-45 tension testing  
other values estimated from literature

Table 5. Comparison of theoretical and experimental  
 $\text{NU}_{xz}$  results.

$[0/0/90]_{16s}$ AS4/3501-6		$[0/0/90]_{16s}$ S2/3501-6	
Theor.	Exp.	Theor.	Exp.
$E_x$	11.71	11.60	5.25
$E_y$	6.6		3.3
$E_z$	1.8		1.5
$\text{NU}_{xy}$	.075	.067	.127
$\text{NU}_{xz}$	.451	.450	.364
$\text{NU}_{yz}$	.47		.38
$G_{xy}$	.87		.98
$G_{xz}$	.73		.78
$G_{yz}$	.63		.64

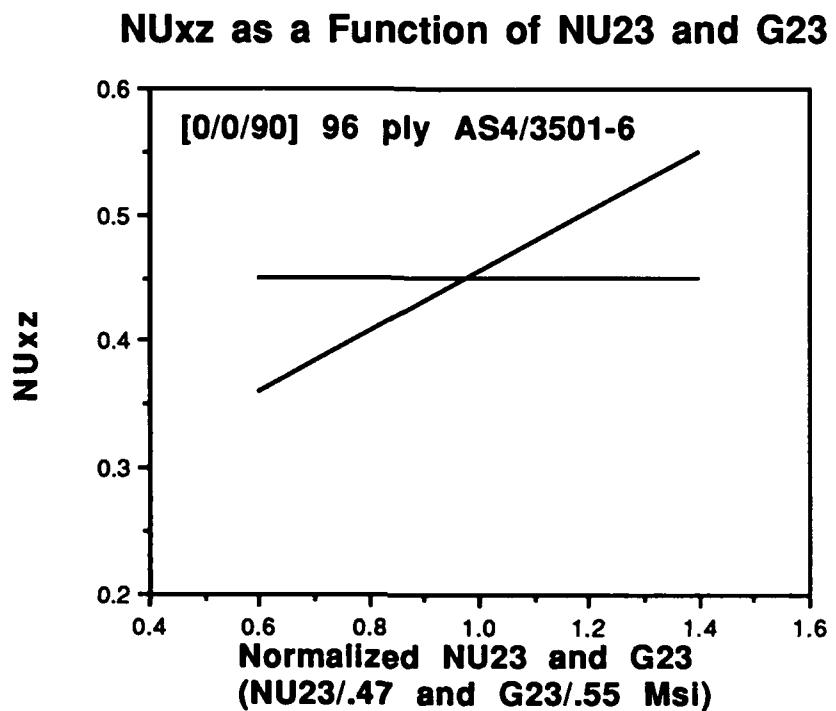


Fig. 11. NU<sub>xz</sub> sensitivity - carbon/epoxy.

### NUxz as a Function of NU23 and G23

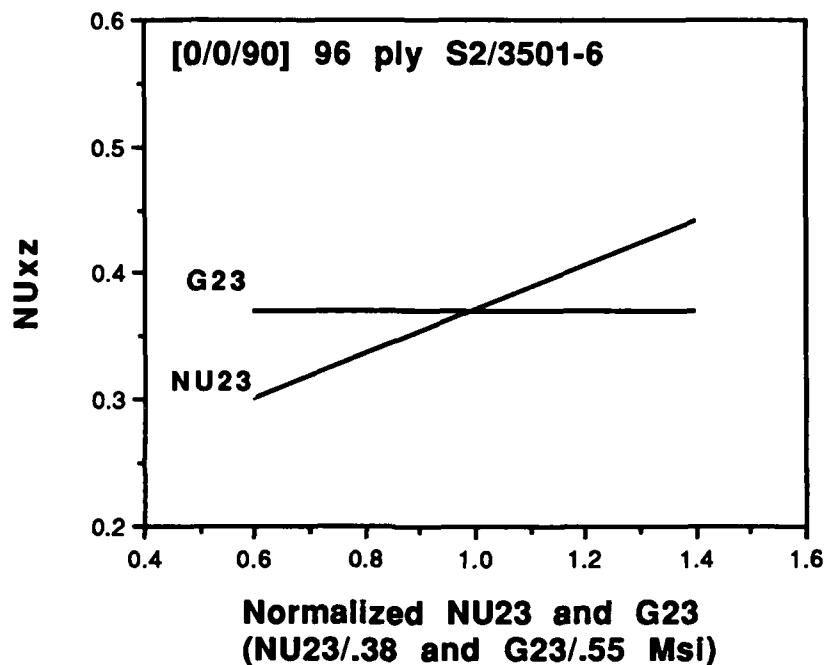


Fig. 12. NU<sub>xz</sub> sensitivity - S2 glass/epoxy.

The results of this comparison show good agreement between theoretically and experimentally determined three-dimensional orthotropic laminate properties. The benchmark thick-section compression data included here correlates well with a closed-form solution that predicts these laminate properties. Since little experimental three-dimensional elastic constant data is available for composite materials, and since such data is costly to develop, the use of theoretical tools to predict these properties is essential. This initial validation of one such tool indicates it may be used for determining the longitudinal moduli and three-dimensional Poisson's ratios for thick composite laminates.

#### CONCLUSIONS

A method for determining the through-thickness strain response of thick composites subjected to compressive loading has been developed and used to determine this response of AS4/epoxy and S2 Glass/epoxy composite materials. This data was used to determine the through-thickness elastic constants of the materials and laminate configurations studied.

The accuracy and utility of three-dimensional models for thick composite materials will be directly related to the accuracy of the material properties used as input for these models. Data from this report has shown that for thick-section unidirectional specimens the elastic constants measured showed good agreement with the assumption of transverse isotropy. Furthermore, for the [0/0/90] laminates evaluated, the values

measured for  $\text{NU}_{xz}$  showed good agreement with values predicted by an analysis that provides all nine elastic constants for orthotropic plates. Additional work validating the prediction of the three-dimensional shear moduli of thick laminated composites using this model is necessary.

#### Acknowledgments

The author would like to acknowledge the support of the DTRC IR/IED program sponsors and in particular the support and encouragement provided by Drs. Dave Moran and Bruce Douglas and Mr. Joe Crisci.

## REFERENCES

1. Camponeschi, E. T., Jr. "Compression of Composite Materials: A Review," David Taylor Research Center Report, DTTC-87-050, November (1987).
2. Timoshenko, S. P. and Gere J. M., Theory of Elastic Stability, McGraw-Hill, New York (1961).
3. Knight, M. "Three-Dimensional Elastic Moduli of Graphite/Epoxy Composites," Journal of Composite Materials, Vol. 16, pp. 153-159 (1982).
4. Trethewey, B. R., Jr., Wilkins, D. J., and Gillespie, J. W., Jr., "Three-Dimensional Elastic Properties of Laminated Composites," CCM Report 89-04, Univ. of DE (1989).
5. Pagano, N. J., "Exact Moduli of Anisotropic Laminates," Mechanics of Composite Materials, Sendeckyj, Ed., pp. 23-44, Academic Press (1984).
6. Kriz, R. D. and Stinchcomb, W. W., "Elastic Moduli of Transversely Isotropic Graphite Fibers and Their Composites," Experimental Mechanics, Vol. 19, No. 2, pp. 41-49 (1979).

INITIAL DISTRIBUTION

Copies	CENTER DISTRIBUTION		
	Copies	Code	Name
12 DTIC			
3 NAVSEA	1	0115	Caplan
1 05M3 (Pinto)			
1 92R (Swan)	1	0113	Douglas
3 NRL	1	17	Krenzke
1 6383 (Badaliance)			
1 6383 (Wolock)	1	172	Rockwell
1 6385 (Chaskelis)			
	1	176	Sykes
1 NSWC			
1 R31 (Augl)	1	1720.2	Phyillaier
1 ONT	1	1720.4	Wiggs
1 225 (Kelly)			
	1	1730.2	Critchfield
1			
Dr. Don Adams	1	2723	Wilhelmi
ME Dept.			
Univ. of Wyoming	1	274	Wang
Laramie, WY 82071			
	1	28	Wacker
1			
Ken Cheverton	1	2801	Crisci
SPARTA Inc.			
4520 Executive Dr., Suite 210	1	2802	Morton
Chicago, IL 60616			
	25	2802	Camponeschi
1			
Dr. Reaz Chaudhuri	1	2803	Cavallaro
Dept. of Civil Eng.			
3220 Merrill Eng. Bldg.	1	284	Fischer
Univ. of Utah			
Salt Lake City, UT 84112	1	2844	Castelli
1			
Dr. H. T. Hahn	1	522.2	TIC (A)
The Pennsylvania State Univ.			
227 Hammond Building	1	522.1	TIC (C)
University Park, PA 16802	1	5231	Office Services

INITIAL DISTRIBUTION (Continued)

1  
K. E. Hofer  
L. J. Broutman & Assoc. Ltd.  
3424 South State St.  
Chicago, IL 60616

1  
Dr. D. Wilkins  
Director, CCM  
University of Delaware  
Newark, DE 19716

1  
Subhash Khatri  
Materials Eng. Dept.  
Drexel Univ.  
Philadelphia, PA 19104

1  
Ms. E. Gail Guynn  
1201 Harvey Road, #24  
College Station, TX 77843

1  
Dr. R Sierakowski  
Chairman, Civil Eng. Dept.  
Ohio State Univ.  
2070 Neil Ave.  
470 Hitchcock Hall  
Columbus, OH 43210

1  
Mr. Jack Woods  
Foster Miller  
350 Second Avenue  
Waltham, MA 02154

1  
K. A. Stubenhofer  
Information Center  
Lord Corp.  
PO Box 10039  
Erie, PA 16514

1  
Mr. Ray Garvey  
Oak Ridge National Laboratory  
P.O. Box 2003  
Oak Ridge, TN 37831-7294

1  
Dr. Steve Yurgartis  
ME Dept.  
Clarkson Univ.  
Potsdam, NY 13676

1  
Mr. Mark Sherman  
Amoco Research Center  
P.O. Box 400  
Naperville, IL 60566

1  
Dr. J. R. Vinson  
Dept. of Mech. Engineering  
Spencer Laboratory  
Univ. of Delaware  
Newark, DE 19716

1  
Dr. Mark Shuart  
Langley Research Center  
Mail Code 190  
Hampton, VA 23665

1  
Dr. R. K. Eby  
Materials Science and Engineering  
102 Maryland Hall  
The Johns Hopkins University  
Baltimore, MD 21218

1  
Dr. Bruce Trethewey  
BASF Structural Materials Inc.  
TPC  
13504-A Southpoint Boulevard  
Charlotte, NC 28217

1  
Dr. R.B. Pipes  
Dean of Engineering  
University of Delaware  
Newark, DE 19716

INITIAL DISTRIBUTION (Continued)

1

Anough Poursartip  
Dept. of Metals & Materials Engineering  
University of British Columbia  
309-6350 Stores Road  
Vancouver, British Columbia  
Canada V6T 1W5

1

John M. Winter, Jr.  
Center for Nondestructive Evaluation  
102 Maryland Hall  
The Johns Hopkins University  
Baltimore, MD 21218

1

Mohamed G. Abdallah, Ph.D., P.E.  
Hercules Incorporated  
Science and Technology Department  
Bacchus Works  
Magna, UT 84044-0098

1

Thomas K. Tsotsis, Ph.D.  
Composite Materials  
CIBA-GEIGY Corporation  
5115 East La Palma Avenue  
Anaheim, CA 92807-2018

1

John H. Bode, Ph.D., P.E.  
Honeywell Inc.  
Armament Systems Division  
MN48-2500  
7225 Northland Drive  
Brooklyn Park, MN 55428

1

Don E. Pettit  
Composites Development Center  
Lockheed  
Aeronautical Systems Company  
D74-72, B369, B6  
Burbank, CA 91520-7004

1

K. Benjamin Su  
E. I. Du Pont De Nemours & Company  
Engineering Technology Laboratory  
Experimental Station - 80304  
Wilmington, DE 19880-0304

1

T. H. Tsiang, Sc.D.  
Lockheed  
Aeronautical Systems Company  
Burbank, CA 91520-4717

1

R. H. Boschan  
Composites Development Center  
Lockheed  
Aeronautical Systems Company  
Burbank, CA 91520-7637

1

Anthony A. Caiazzo, P.E.  
Materials Science Corporation  
Gwynedd Plaza II  
Spring House, PA 19477

1

Douglas S. Cairns, Ph.D.  
Hercules Incorporated  
Science & Technology Department  
Bacchus Works  
Magna, UT 84044-0098

1

Dr. David Cohen  
Hercules Aerospace Company  
Missiles, Ordnance & Space Group  
Bacchus Works  
Magna, UT 84044-0098

1

Ori Ishai, D.Sc.  
Professor, Faculty of Mechanical  
Engineering  
Technion - Israel Institute of  
Technology  
Technion, Haifa 32000, Israel

1

John Morton, D. Phil  
Engineering Science & Mechanics  
Department  
Virginia Polytechnic Institute  
and State University  
Blacksburg, VA 24061

1  
Vasilios Peros  
Martin Marietta  
Aero & Naval Systems  
103 Chesapeake Park Plaza  
Baltimore, MD 21220

1  
John W. Gillespie, Jr., Ph.D.  
Center for Composite Materials  
Composites Manufacturing Science Laboratory  
University of Delaware  
Newark, DE 19716

1  
Dr. Donald L. Hunston  
Polymer Composites Group  
Polymers Division  
National Institute of Standards  
and Technology  
Building 224, Room A209  
Gaithersburg, MD 20899

1  
Prof. A. J. Vizzini  
The University of Maryland  
College of Engineering  
Department of Aerospace Engineering  
College Park, MD 20742

1  
Dr. Fuh-Gwo Yuan  
Department of Mechanical  
& Aerospace Engineering  
North Carolina State University  
Raleigh, NC 27695-7910